



# An introduction to GPS radio occultation and its use in NWP

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# An introduction to GPS radio occultation and its use in NWP

- Radio occultation (RO) – introduction
- Variational data assimilation – introduction
- Assimilation options for RO data
- Some issues for this Workshop



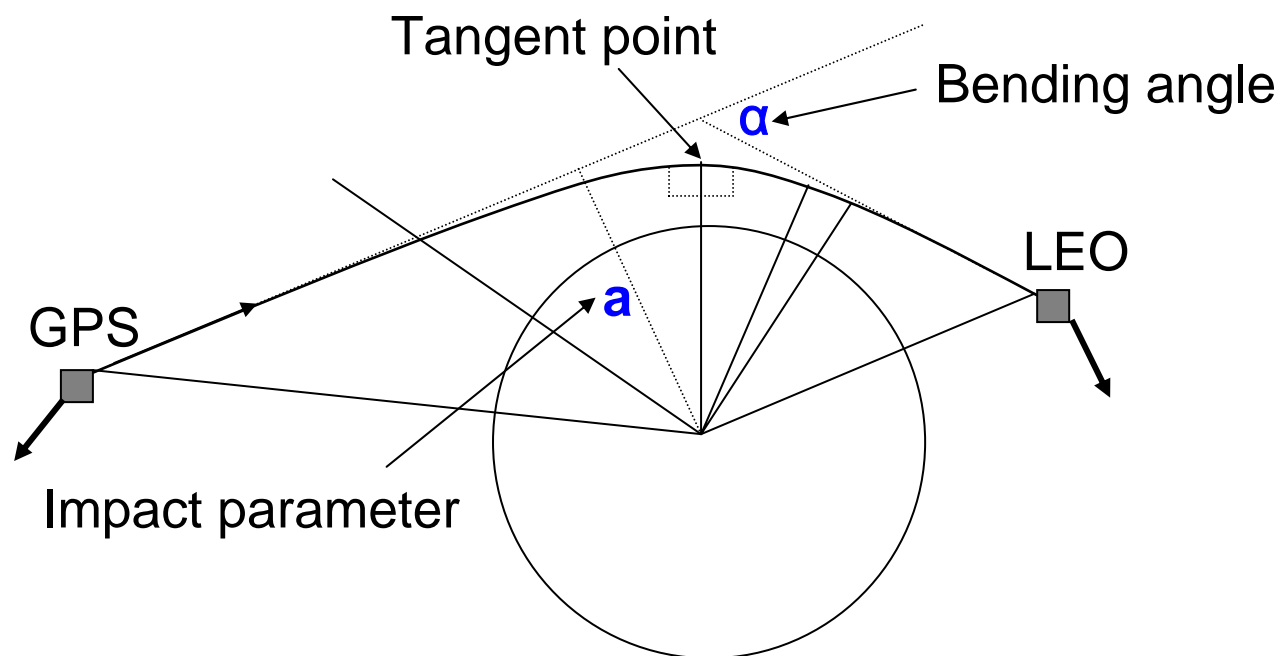
# GPS – the source data

## The Global Positioning System (GPS)

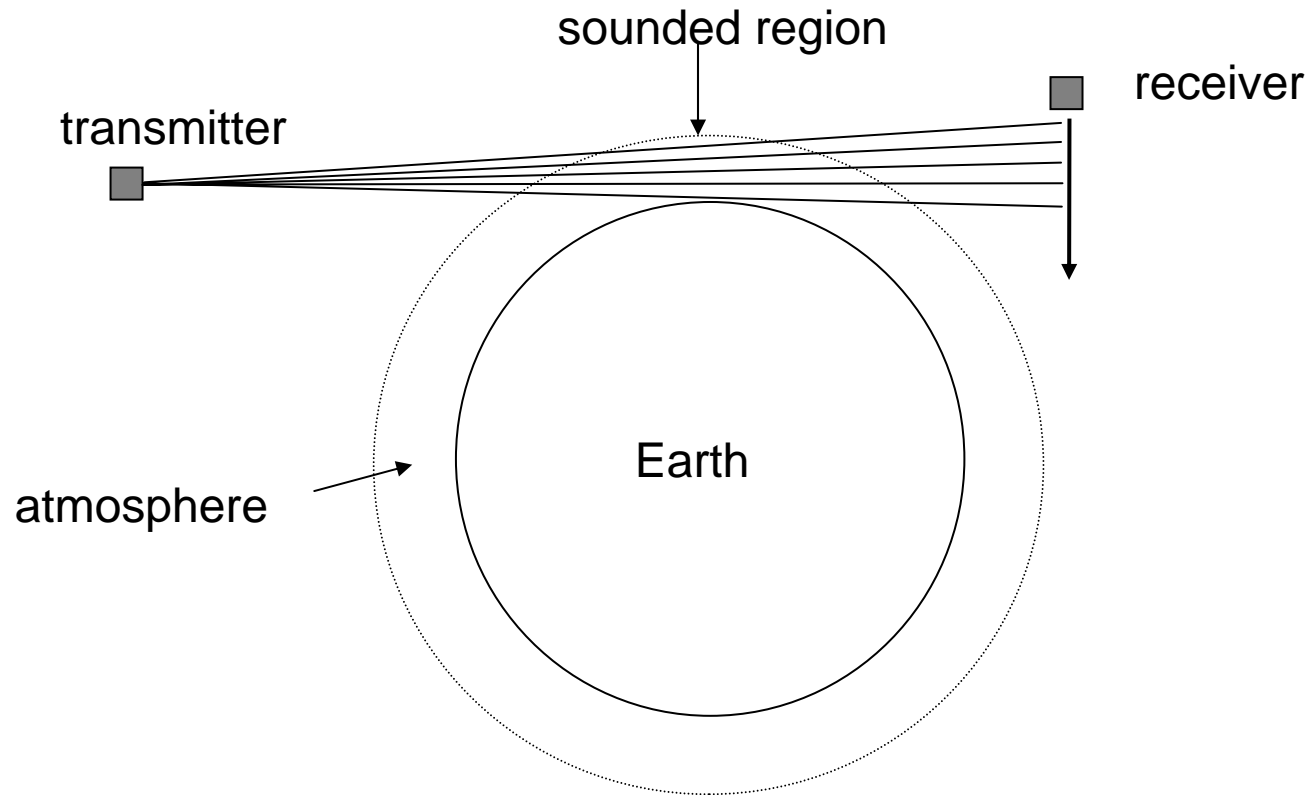
- multi-purpose - applications in positioning, navigation, surveying, ...
- nominal GPS network = 24 satellites
- near polar orbit - height ~20000 km
- allows high-accuracy positioning of low Earth orbiters (LEOs)
- source of refracted radio signals for radio occultation



# Geometry of a radio occultation measurement



# An occultation



A sounding from 60 km to the surface takes ~60s



# Atmospheric refraction: the physics

Refractivity gradients caused by gradients in:

- density (pressure and temperature)
- water vapour
- electron density
- (liquid water)

$$N = \kappa_1 p / T + \kappa_2 e / T^2 + \kappa_3 n_e / f^2 + \kappa_4 W$$

“dry”                      “moist”                      ionosphere                      “scattering”

N = refractivity =  $(n - 1) \times 10^6$

p = pressure

e = water vapour pressure

f = frequency

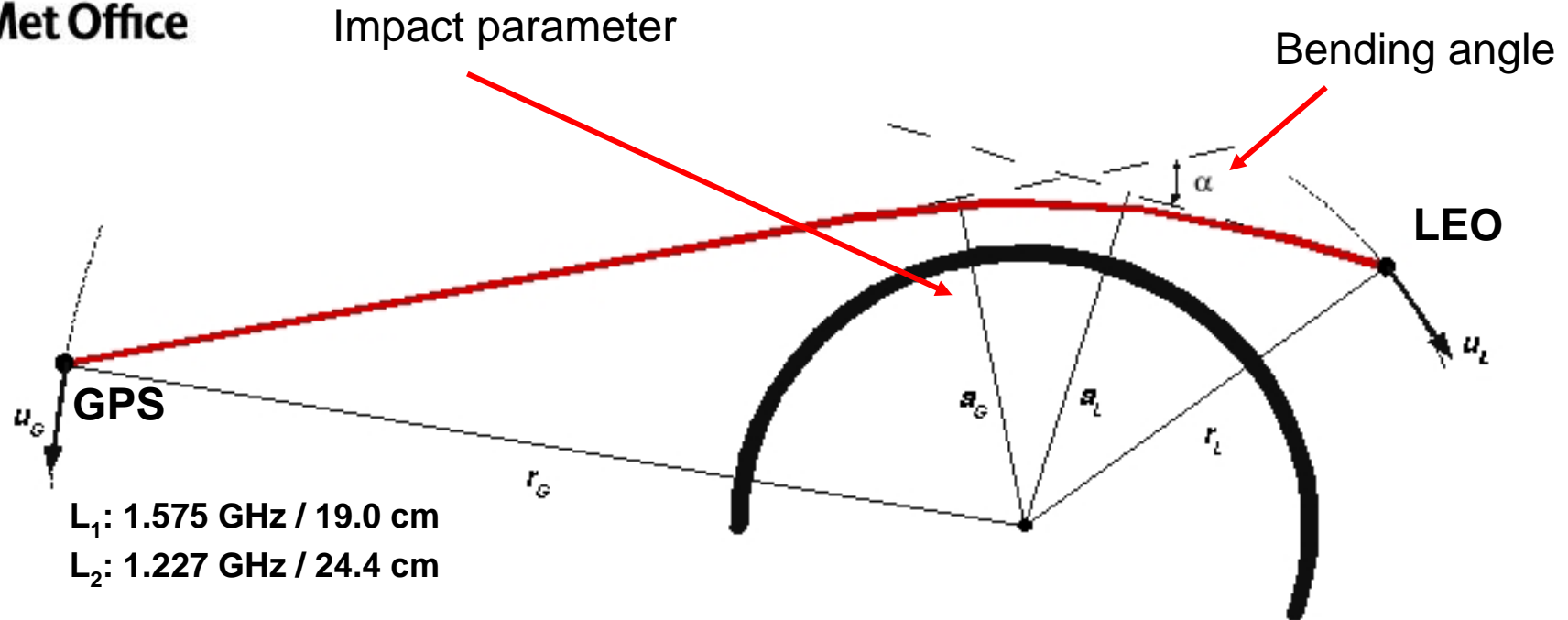
n = refractive index

T = temperature

$n_e$  = electron density

W = liquid water density

# From bending angle to density



$$\ln(n(a)) = \frac{1}{\pi} \int_a^\infty \frac{\alpha(a')}{\sqrt{a'^2 - a^2}} da'$$

Refractive index

$$N = (n - 1) \times 10^6 = \kappa_1 \frac{p}{T} + \kappa_2 \frac{e}{T^2}$$

Refractivity



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# Features of RO measurements

- globally distributed
- temperature in stratosphere and upper troposphere, and ...
- humidity in lower troposphere
- high vertical resolution: 0.5 - 1 km
- low horizontal resolution: ~ 200 km
- high accuracy:
  - random errors <1K
  - systematic errors <0.2K - to be demonstrated in practice
- “all-weather”
- relatively inexpensive
- receivers x transmitters → space/time sampling





# Radio occultation missions

## Past:

- GPS/MET: 1995-7 1 selected periods only

## Present:

- CHAMP: 2000- 1 continuous since 2001, nrt since 2006
- GRACE-A: 2002- 1 continuous since 2003, nrt since 2006
- COSMIC: 2006- 6 quasi-operational demonstration
- GRAS: 2006- 1 operational 2008

## Future:

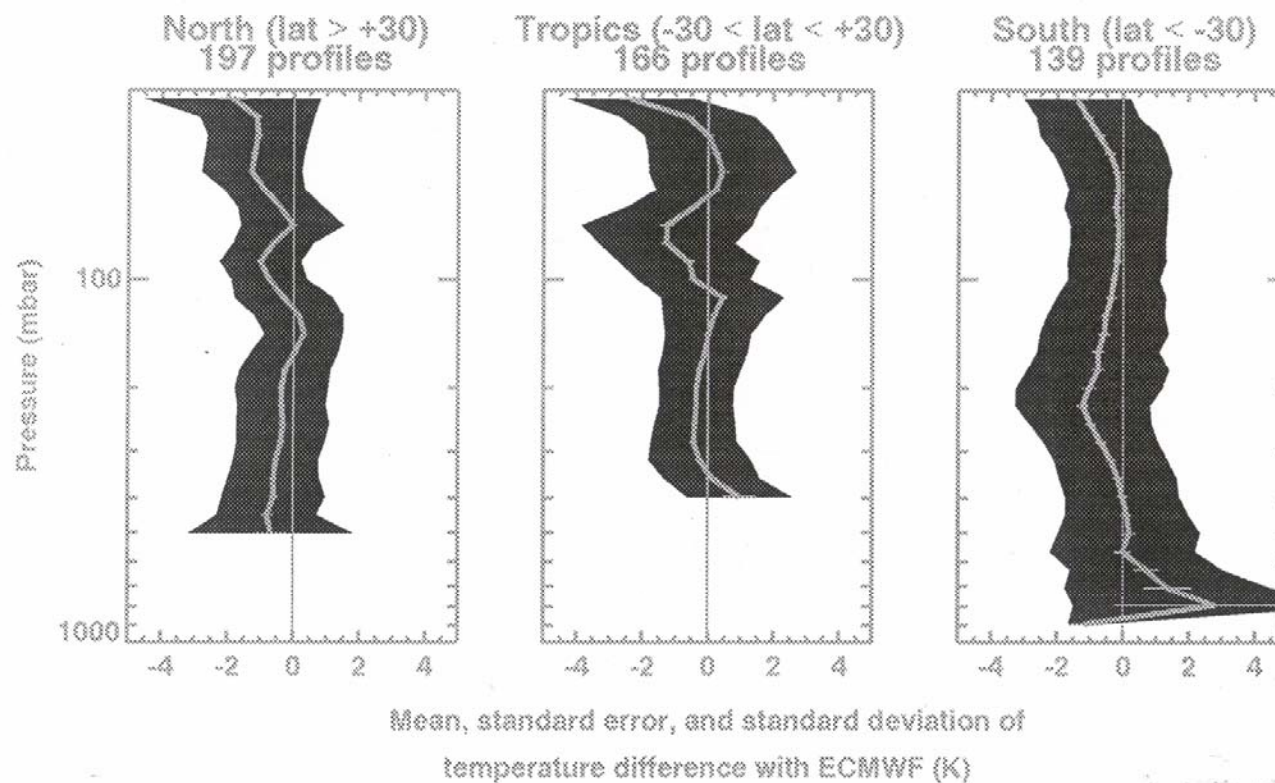
- ???



# GPS/MET – early results

## Comparison of GPS/MET Retrievals with ECMWF

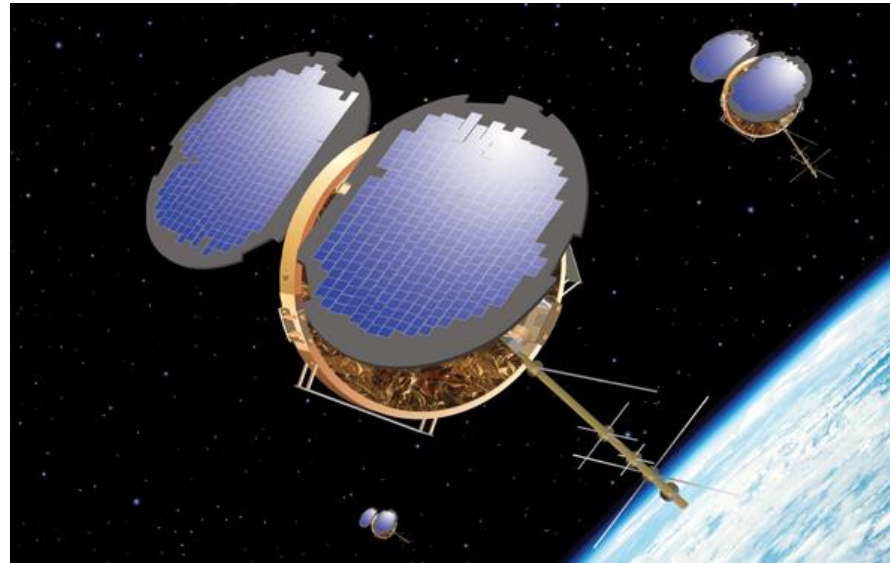
### Summer AS-off Period



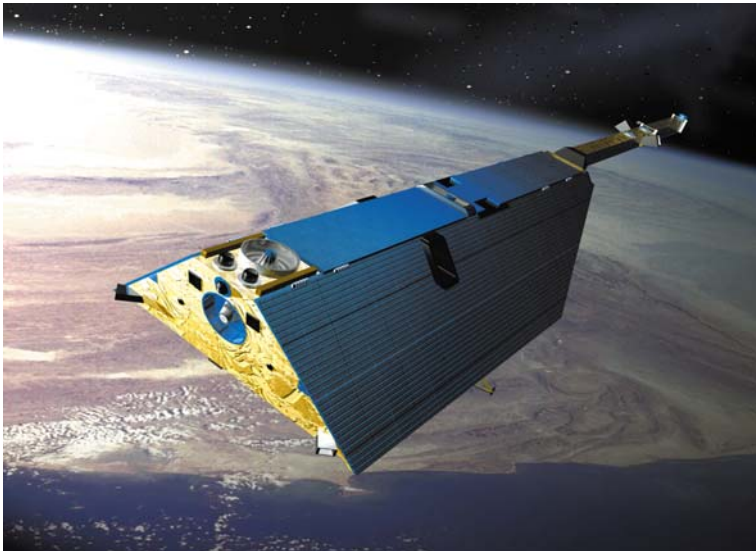
JPL: Kursinski, Hajj, Bertiger, Leroy, Romans, Schofield, et al. (6 December 1995)



COSMIC

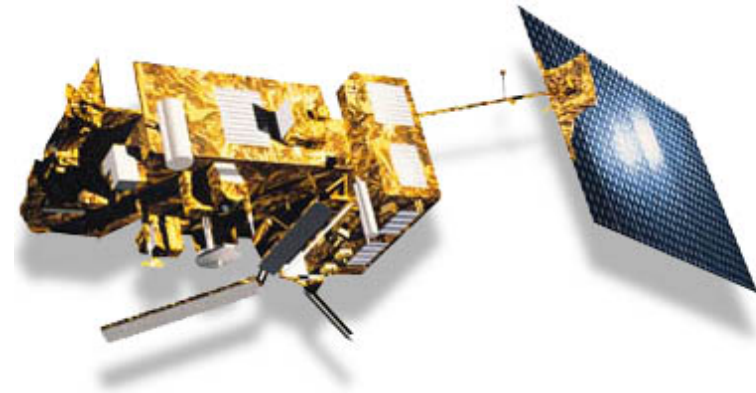


CHAMP



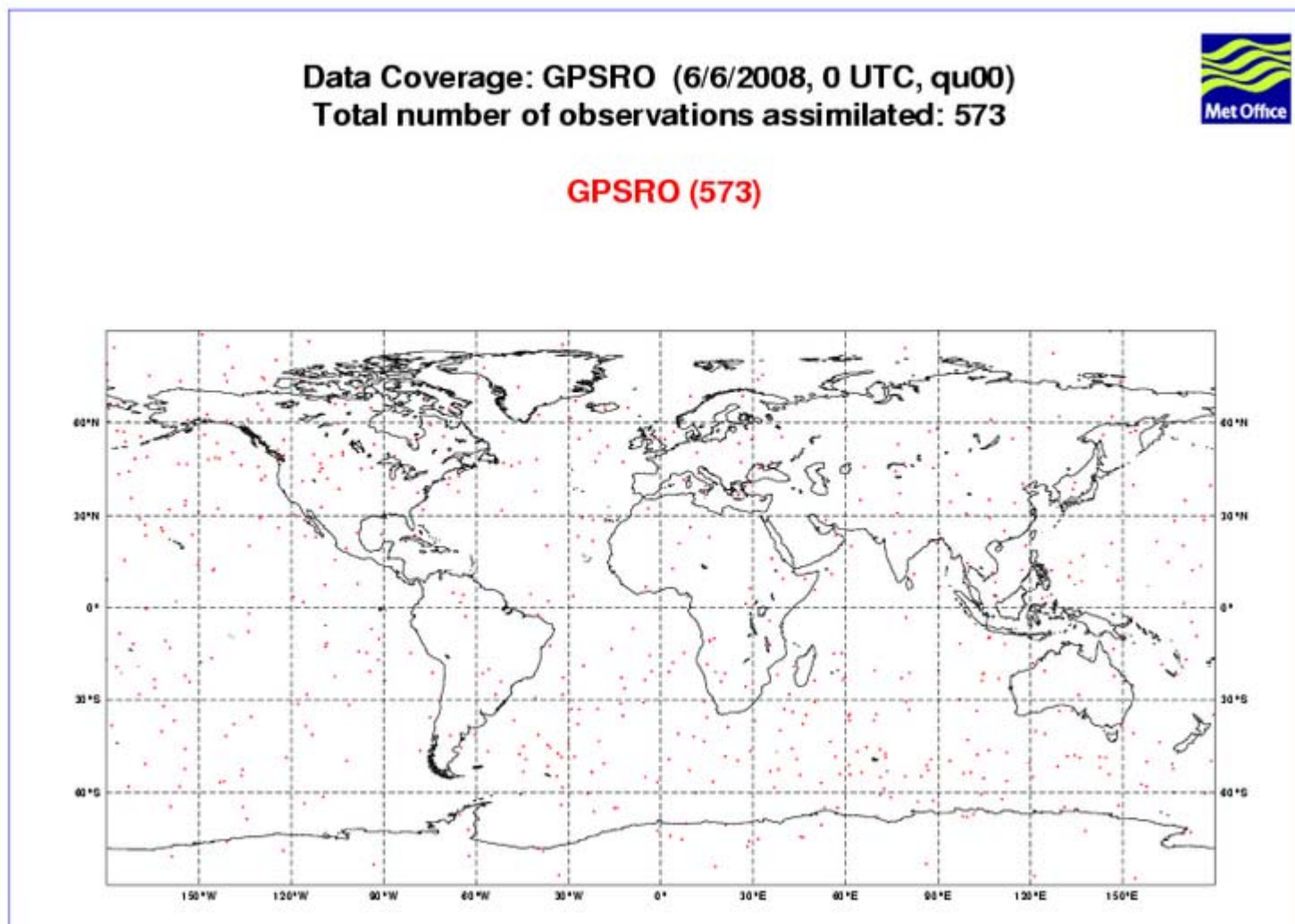
© Crown copyright 2007

Metop/GRAS





# COSMIC data coverage in 6 hours





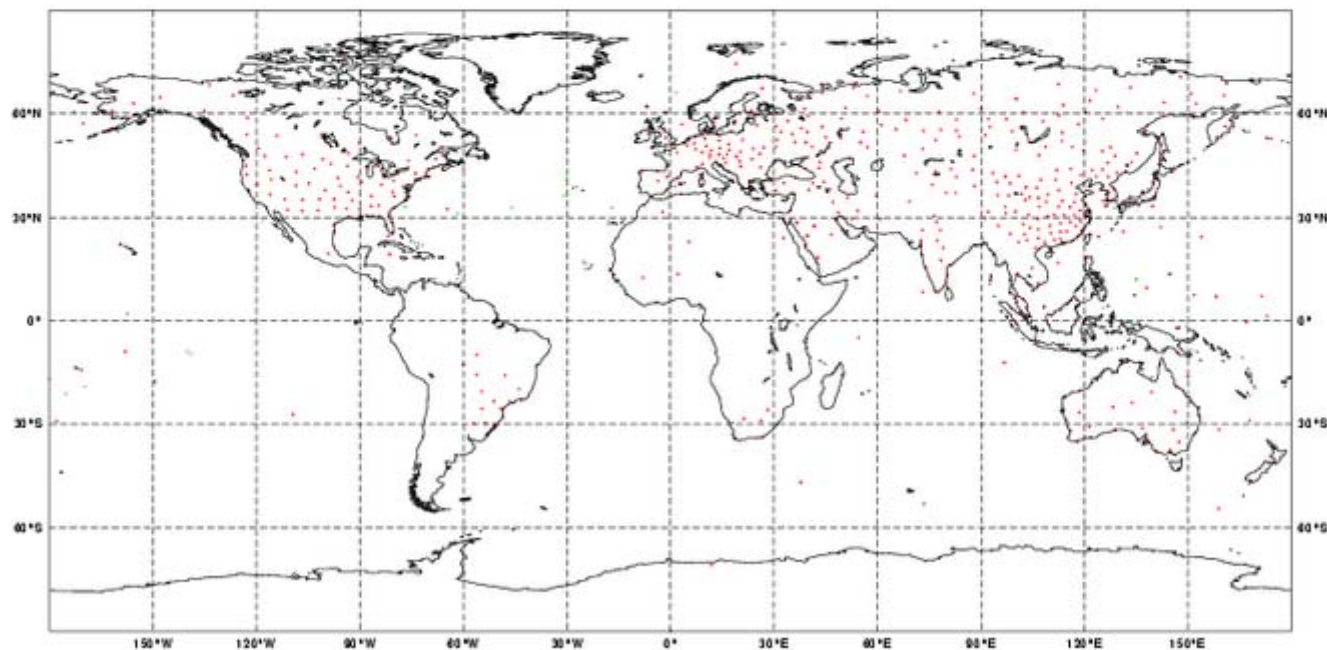


... compared with sondes

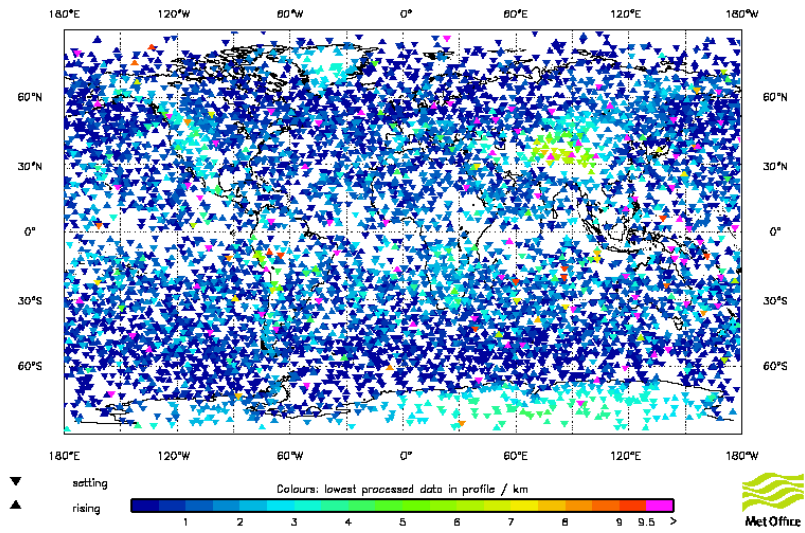
Data Coverage: Sonde (6/6/2008, 0 UTC, qu00)  
Total number of observations assimilated: 618



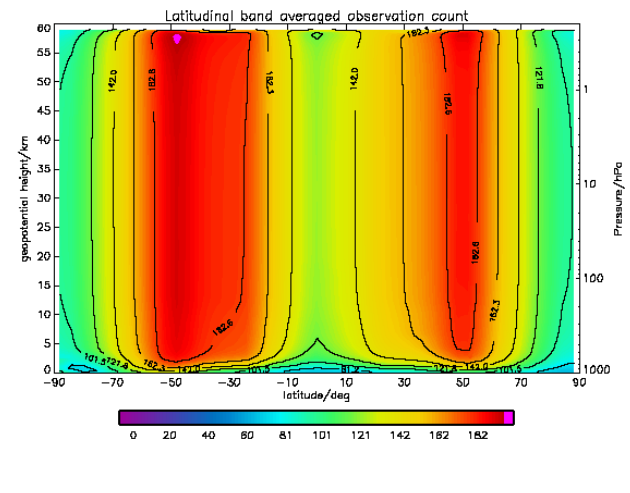
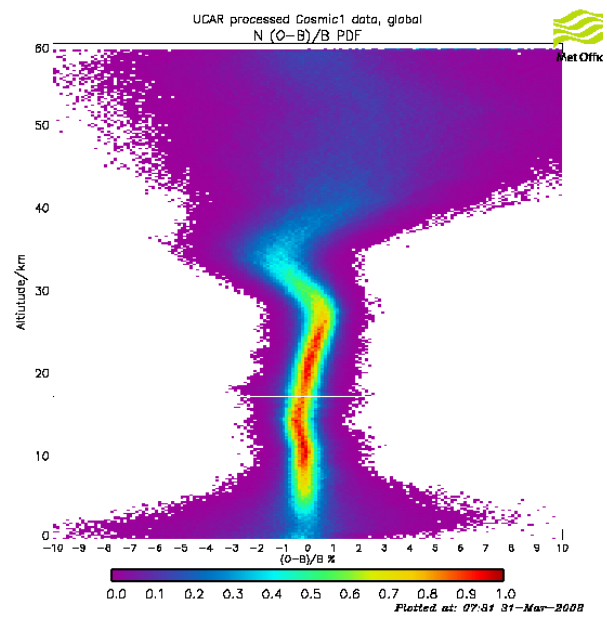
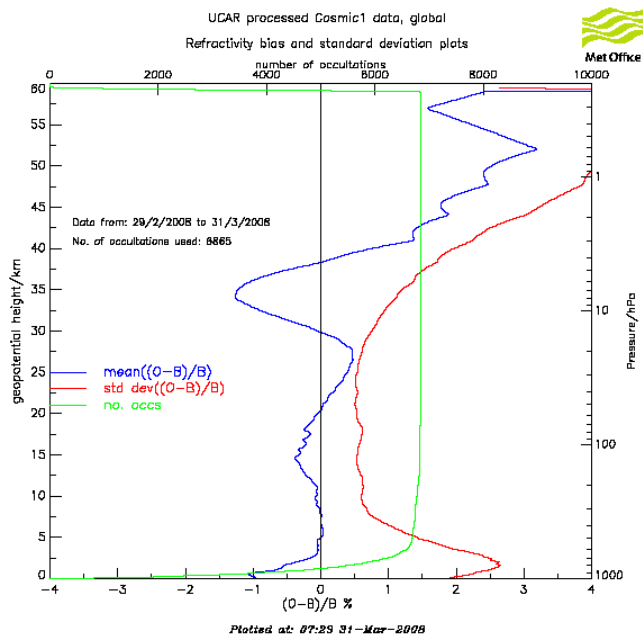
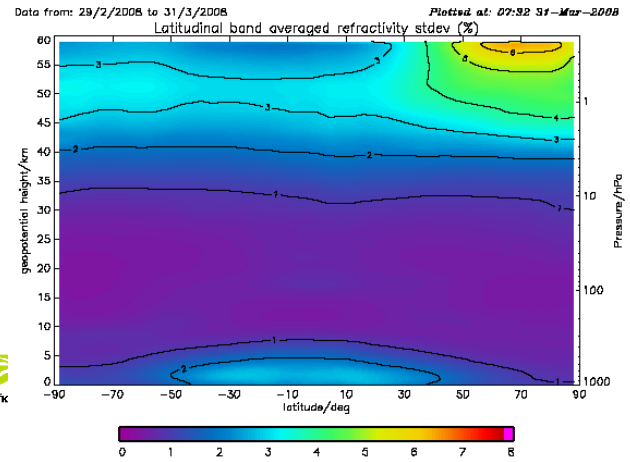
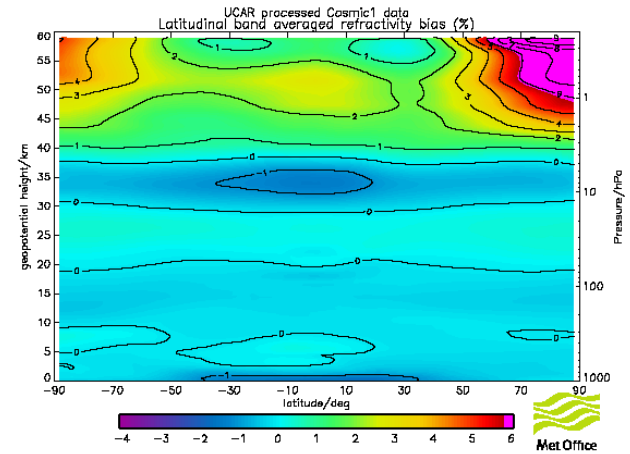
TEMP LAND (609) TEMP SHIP (9) TEMP MOBILE (0)



Map of all Cosmic1 UCAR occultations with lowest processed altitude shown by colour  
 Data from: 29/2/2008 to 31/3/2008  
 Total no. occs: 6865 No. rising: 2523 No. setting: 4342



# GRAS SAF Monitoring





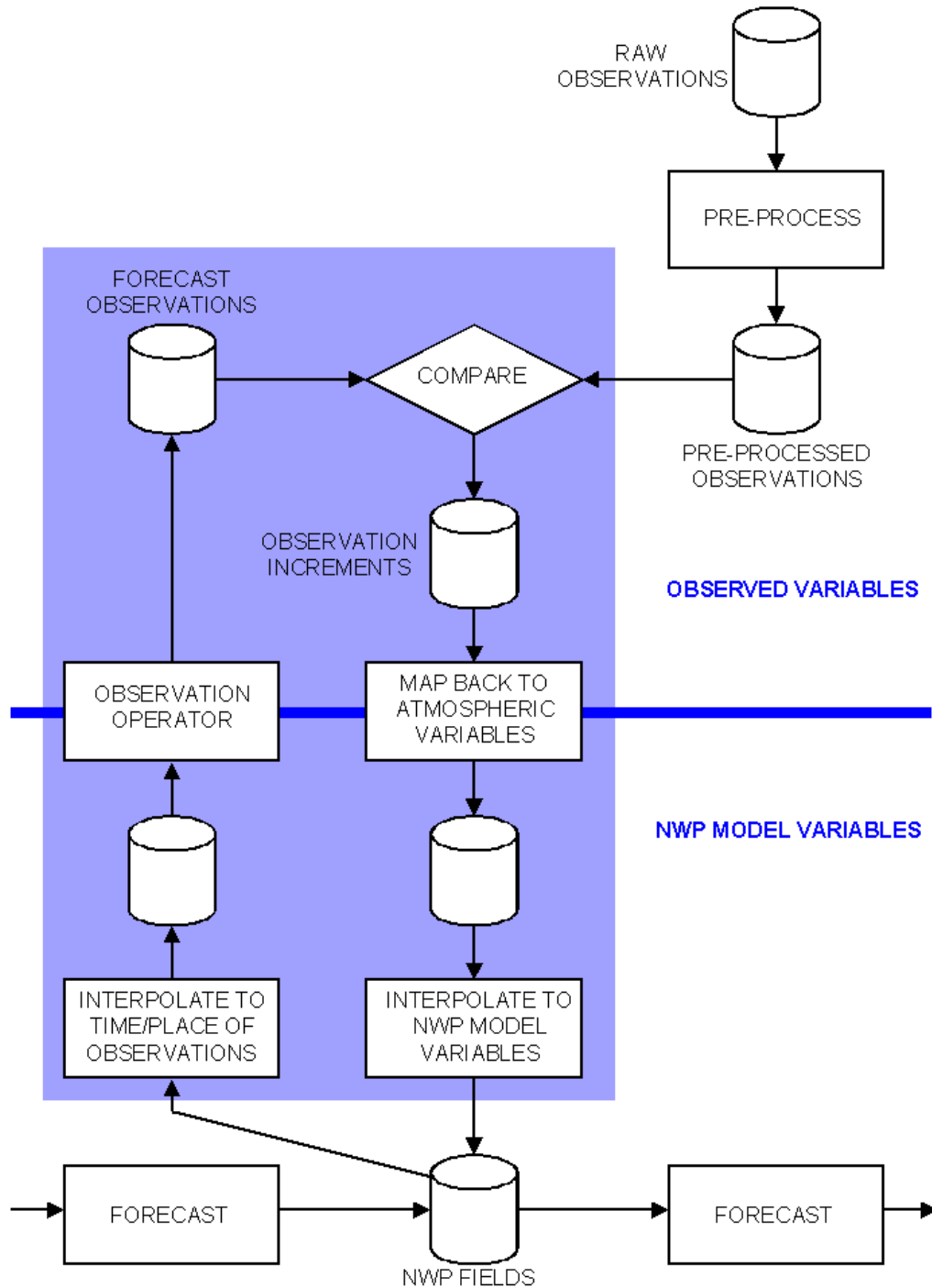
# Variational data assimilation

Minimize:

$$\mathcal{J}[x] = \frac{1}{2} (x-x^b)^T B^{-1} (x-x^b) + \frac{1}{2} (y^o-H[x])^T (E+F)^{-1} (y^o-H[x])$$

$x$	NWP model state
$x^b$	background estimate of $x$ (short-range forecast)
$B$	its error covariance
$y^o$	vector of measurements
$H[...]$	“observation operator ” or “forward model” mapping state $x$ into “measurement space”
$E$	error covariance of measurements
$F$	error covariance of forward model.

$$\nabla_x \mathcal{J}[x]^T = B^{-1} (x-x^b) - \nabla_x H[x]^T (E+F)^{-1} (y^o-H(x)) = 0$$



# Assimilating observations into a NWP model





# Assimilation options for RO data

## Options:

- (1) assimilate retrieved profiles of temperature and humidity
- (2) assimilate retrieved profile of refractivity,  $N(z)$
- (3) assimilate measured bending angles,  $\alpha(a)$ , directly

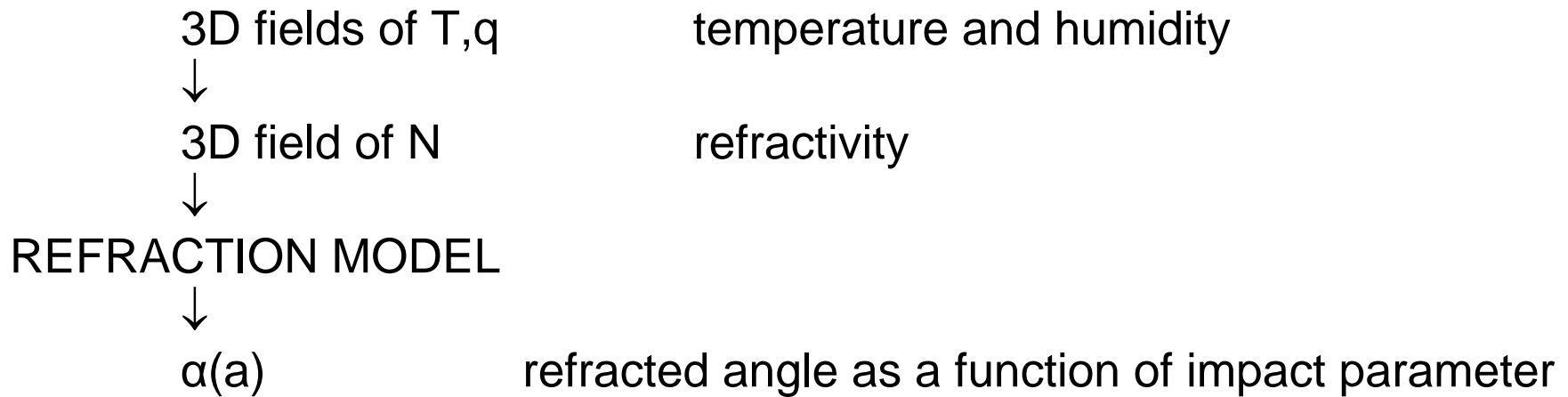
## Special problems with RO data:

- non-separability of temperature and humidity
  - addressed by (2) and (3)
- limited horizontal resolution / problems of horizontal gradients
  - partially addressed by (3)



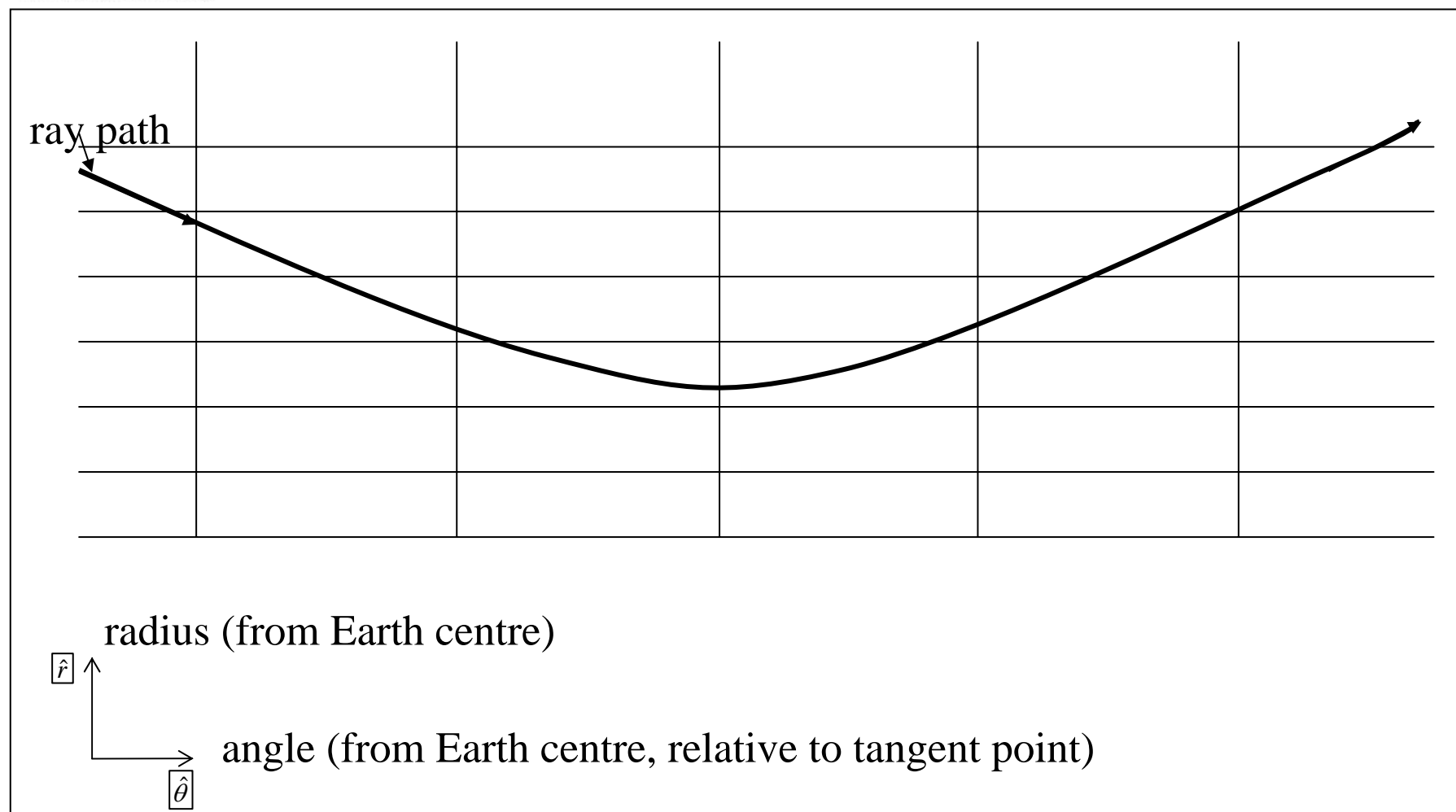
# Forward modelling for RO data

Forward problem:



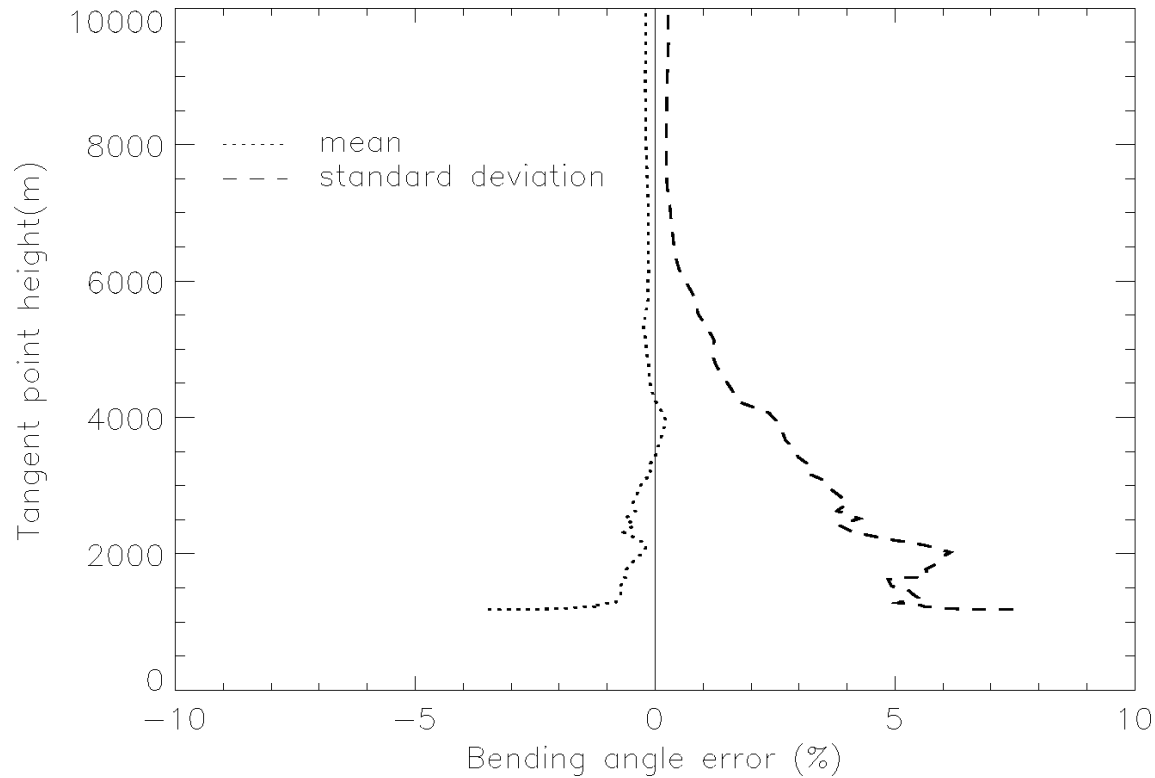


## 2D fast forward model of refraction in plane of occultation





## RO forward model: accuracy



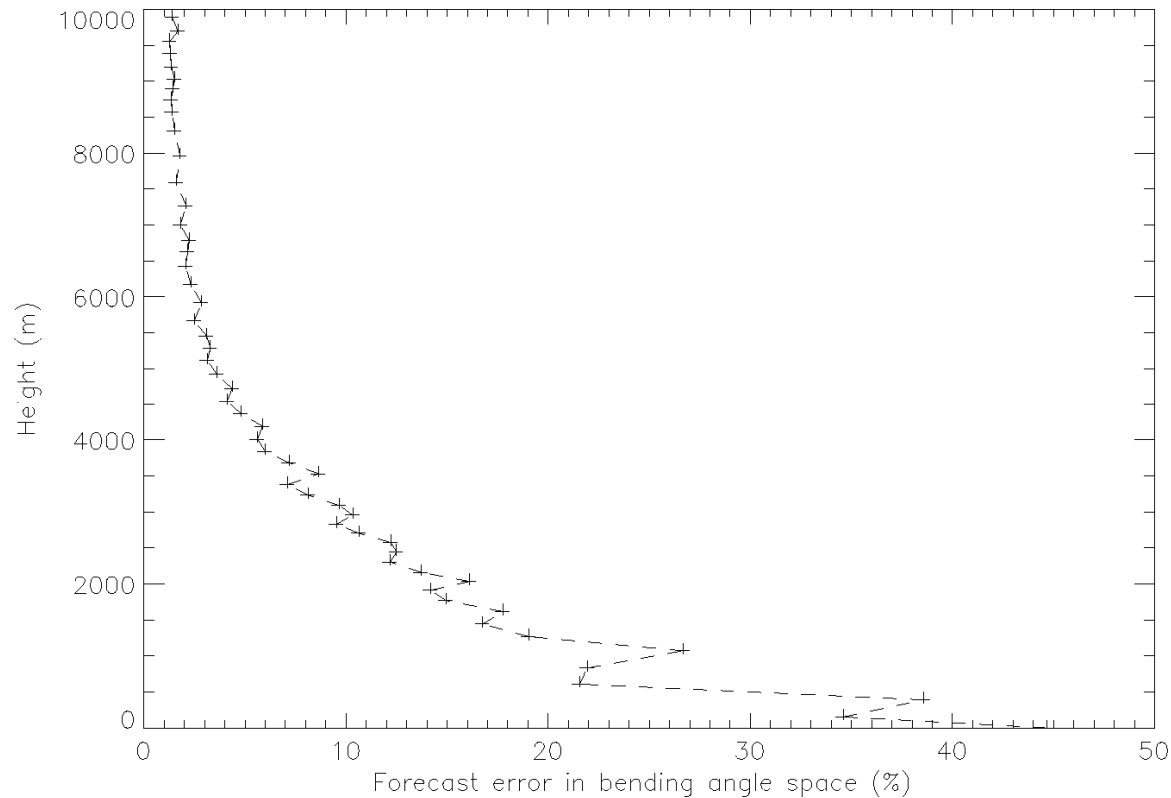
Comparisons against a 3D ray tracer for simulations in the domain of the Met Office mesoscale model. 160 cases.

Healy and Eyre, 2003.

Largest source of error - using impact parameter to derive tangent point height.



# Forecast errors mapped into bending angle space



Diagonal of  
 $\nabla_x H[x] \cdot B \cdot \nabla_x H[x]^T$

Significantly larger  
than the forward  
model errors

Healy and Eyre,  
2003.



## Information content of RO data

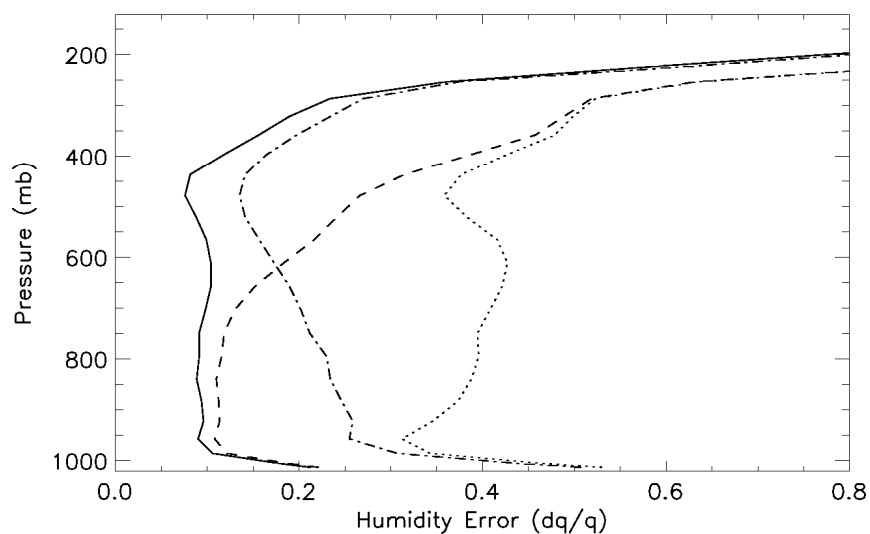
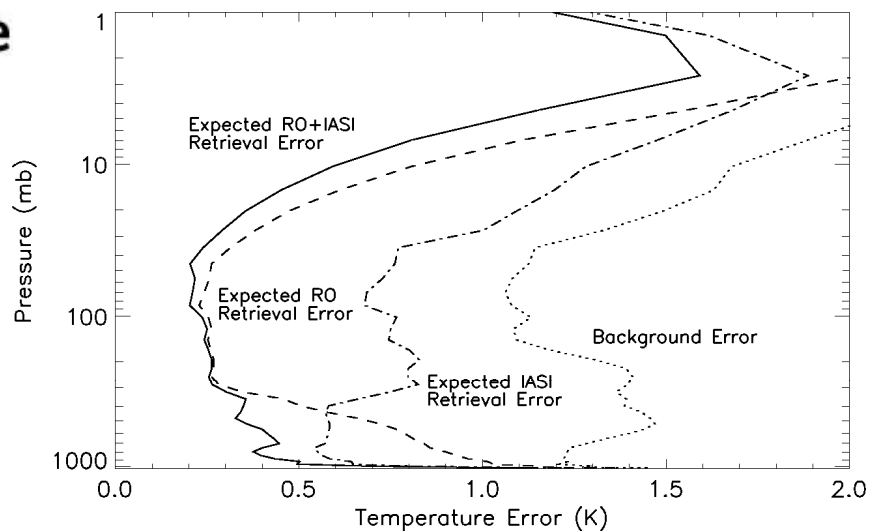
- Information is always relative - relative to what you already know, the “prior” information
- For NWP, the information content of an observation depends on the accuracy of the “background” information from a short-range forecast:

$$A^{-1} = B^{-1} + \nabla_x H[x]^T \cdot (E+F)^{-1} \cdot \nabla_x H[x]$$

retrieval "accuracy" = background "accuracy" + measurement "accuracy"



# Information content: RO and IASI



Collard and Healy,  
QJRMS 2003



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## Summary

### Radio occultation measurements:

- sensitive to vertical gradients of atmospheric refractivity
- → and hence to atmospheric profiles of temperature and humidity
- used to study atmospheres of other planets since mid-1960s
- powerful new technique for sounding the Earth's atmosphere with high vertical resolution and accuracy
- great potential for NWP and climate monitoring
- temperature and humidity effects cannot be separated unambiguously, but ...
- variational data assimilation allows optimal exploitation in NWP





# Some issues for this Workshop

## NWP

- Early impacts very good
- What is limiting impact? – relative biases?

## Climate

- Stability – truly self-calibrating?

## Other applications

- PBL information – NWP and other applications
- Reflected signals

## Future systems

- How many receivers x transmitters needed? - OSSEs?
- How do we ensure follow-on missions?



Thank you! Questions?